Systems of Linear Equations

- 1. The sum of two numbers is 17, and their difference is 21. Find the two numbers.
- 2. The sum of two numbers is 35, and their difference is 27. Find the two numbers.
- 3. A total of 1,096 people attended the Beach Boys concert. Reserved seats cost \$25 each and general admission seats cost \$20 each. If \$26,170 was collected, how many of each type of seat were sold?
- 4. There were 311 tickets sold for a soccer game, some for students and some for non-students. Student tickets cost 25¢ each and non-student tickets cost 75¢ each. The total receipts were \$108.75. How many of each type of ticket were sold?
- 5. Adam wishes to mix 30 lb of candy worth \$6 per lb with candy worth \$3 per lb to get a mixture worth \$5 per lb. How much of the \$3 candy should be used?
- 6. A popular fruit drink is made by mixing fruit juice and soda. Such a mixture with 50% juice is to be mixed with another mixture that is 30% juice to get 100 liters of a mixture which is 45% juice. How much of each should be used?
- 7. A freight train and an express train leave towns 390 km apart, traveling toward one another. The express train travels 30 km/hr faster than the freight train. They pass one another 3 hrs later. What are their speeds?
- 8. Two cars start out from the same spot and travel in opposite directions. At the end of 6 hrs, they are 690 km apart. If one car travels 15 km/hr faster than the other, what are their speeds?
- 9. A train travels 150 km in the same time that a plane covers 400 km. If the speed of the plane is 20 km/hr less than 3 times the speed of the train, find both speeds.
- 10. In his motorboat, Tom travels upstream at top speed to his favorite fishing spot, a distance of 18 mi, in 1 hr. Returning, he finds that the trip downstream, still at top speed, takes only ¾ hr. What is the speed of the current? What is the speed of Tom's boat in still water?
- 11. A chemist needs 10 liters of a 24% alcohol solution. She has on hand a 30% alcohol solution and an 18% alcohol solution. How many liters of each should be mixed to get the required solution?
- 12. A supplier of poultry sells 20 turkeys and 8 chickens for \$74. He also sells 15 turkeys and 24 chickens for \$87. Find the cost of a turkey and the cost of a chicken.
- 13. Ray is a building contractor. If he hires 8 brick layers and 2 roofers, his daily payroll is \$960, while 10 brick layers and 5 roofers require a daily payroll of \$1,500. Find the daily wage of a brick layer and the daily wage of a roofer.
- 14. During summer vacation Hector and Ann earned a total of \$6,496. Hector worked 8 days less than Ann and earned \$4 per day less. Find the number of days he worked and the daily wage made, if the total number of days worked by both was 72.

- 15. A bank teller has ten-dollar bills and twenty-dollar bills. He has 25 more twenties than tens. The value of the bills is \$2,900. How many of each kind does he have?
- 16. George plans to invest \$30,000 he won in a lottery. With part of the money he buys a mutual fund, paying 4.5% a year. The rest he invests in utility bonds paying 5% per year. The first year his investments bring a return of \$1,410. How much is invested at each rate?
- 17. How much milk that is 3% butterfat should be mixed with milk that is 18% butterfat to get 25 gal of milk that is 4.8% butterfat?
- 18. Sweet's Candy Store is offering a special mix for Valentines's Day. Ms. Sweet will mix some \$2 per pound candy with some \$1 per pound candy to get 50 pounds of mix that she will sell at \$1.30 per pound. How many pounds of each should be used?
- 19. To start a new business, Mark borrowed money from two financial institutions. One loan was at 7% interest and the other was for one-third as much money at 8% interest. How much did he borrow at each rate if the total amount of annual interest was \$1,160?
- 20. Susan has invested a total of \$20,000 in two ways. Part of the money is in certificates of deposit paying 3.75% interest, while the rest is in municipal bonds that pay 8.2% interest. How much is there in each account if the total annual interest is \$1,417.50?
- 21. A botanist has patented a successful type of plant food that contains two chemicals, X and Y. Eight hundred kg of these chemicals will be used to make a batch of the food, and the ratio of X to Y must be 3 to 2. How much of each chemical should be used?
- 22. A manufacturer of portable CD players shipped 200 of the players to its two Quebec warehouses. It cost \$3 per unit to ship to Warehouse A, and \$2.50 per unit to ship to Warehouse B. If the total shipping cost was \$537.50, how many were shipped to each warehouse?
- 23. Octane ratings show the percent of isooctane in gasoline. An octane rating of 98, for example, indicates a gasoline that is 98% isooctane. Find the number of gal of 98-octane gasoline and 92-octane gasoline that must be mixed to produce 40 gal of 94-octane gasoline.
- 24. A truck radiator holds 24 liters of fluid. How much pure antifreeze must be added to a mixture that is 4% antifreeze in order to fill the radiator with a mixture that is 20% antifreeze?
- 25. On a 10-day trip Ed rented a car for \$31 a day at weekend rates and \$40 a day at weekday rates. If his rental bill was \$364, how many days did he rent at each rate?
- 26. In an election, one candidate received 135 more votes than the other. The total number of votes cast in election was 1,215. Find the number of votes received by each candidate.

Selected Answers

- **1** 19 and –2
- 3 850 reserved; 246 general admission
- 5 15 lb
- 7 freight: 50 km/hr; express: 80 km/hr
- 9 plane: 160 km/hr; train 60 km/hr
- **11** 5 l of 30%; 5 l of 18%
- **13** \$90 for a brick layer; \$120 for a roofer

- **15** 80 tens; 105 twenties
- **17** 22 gal of 3%; 3 gal of 18%
- **19** \$12,000 at 7%; \$4,000 at 8%
- 21 480 kg of X; 320 kg of Y
- **23** 13 1 /₃ gal of 98 octane; 26 2 /₃ gal of 92 octane
- 25 4 days at weekend rate; 6 days at weekday rate